

## Symbols in Map Projections – A Proposal for Standardization, Ver. 2

M. Lapaine, 7 July 2019

Comments were given by Frank Canters, Dražen Tutić, Nedjeljko Frančula, Daniel danna Strebe, Clifford J. Mugnier, Temenoujka Bandrova, Bojan Šavrić, Doug McIlroy

$\alpha$

azimuth, as angle measured clockwise from the north

$a$

semimajor axis of the ellipsoid of reference

$b$

semiminor axis of the ellipsoid of reference

$e$

(1) first eccentricity of the ellipsoid =  $\sqrt{1 - \frac{b^2}{a^2}}$

(2) base of natural logarithms, where  $e \approx 2.71828$

$e'$

second eccentricity of the ellipsoid =  $\sqrt{\frac{a^2}{b^2} - 1}$

*f*

flattening of the ellipsoid =  $\frac{a-b}{a}$

*f'*

second flattening of the ellipsoid =  $\frac{a-b}{b}$

*h*

relative scale factor along a meridian of longitude

*k*

relative scale factor along a parallel of latitude

*n*

(1) cone constant on conic projections, i.e. the ratio of the angle between images of meridians to the true angle

(2) the third flattening of the ellipsoid =  $\frac{a-b}{a+b}$

*R*

radius of the sphere

*S*

surface area

$x$

(1) first coordinate in a plane or spatial rectangular coordinate system

(2) rectangular coordinate: distance to the right of the vertical line ( $y$  axis) passing through the origin or center of a projection (if negative, it is distance to the left). In practice, a "false"  $x$  or "false easting" is frequently added to all values of  $x$  to eliminate negative numbers. Note: Many texts use  $x$  and  $y$  axes interchanged, not rotated, from this convention.

$y$

(1) second coordinate in a plane or spatial rectangular coordinate system

(2) rectangular coordinate: distance above the horizontal line ( $x$  axis) passing through the origin or center of a projection (if negative, it is distance below). In practice, a "false"  $y$  or "false northing" is frequently added to all values of  $y$  to eliminate negative numbers.

$z$

(1) third coordinate in a spatila coordinate system

(2) complex number

(3) zenithal distance from North Pole of latitude  $\varphi$ , i.e.  $90^\circ - \varphi$ , where  $\varphi$  is latitude. Known also as colatitude

$\ln$

natural logarithm, i.e. logarithm to base  $e$ , where  $e \approx 2.71828$ . Note the difference to the first eccentricity of the ellipsoid.

$\delta$

angle measured counterclockwise from the central meridian, rotating about the center of the latitude circles on a normal aspect conic or azimuthal projection

$\theta$

smaller of two angles of intersection between meridian and parallel in a plane of projection

$\lambda$

longitude. Longitude values are positive east of Greenwich (or another prime meridian). For longitude west of Greenwich, use negative value.

$\lambda_0$

longitude east of Greenwich of the central meridian of the map (for west longitude use a negative value), or longitude chosen as a parameter to define the origin of rectangular coordinates for a projection

$\lambda'$

transformed longitude east of the new prime meridian, when graticule is rotated on the globe

$\rho$

radius of latitude circle on normal aspect conic or azimuthal projection

$\varphi$

latitude. Latitude values are positive north of the equator. For latitude south of the equator, use negative value.

$\varphi_0$

middle latitude, or latitude chosen as a parameter to define the origin of rectangular coordinates for a projection

$\varphi'$

transformed latitude relative to the new poles and equator when the graticule is rotated on the globe

$\varphi_1, \varphi_2$

standard parallels of latitude for projections with two standard parallels. These are true to scale at any point ( $h=k=1$ )

$\varphi_1$  (without  $\varphi_2$ )

single standard parallel. It is true to scale at any point ( $h=k=1$ )

$\omega$

maximum angular distortion at a given point on a projection,  $\sin \frac{\omega}{2} = \frac{a-b}{a+b}$

$M$

radius of curvature at a point on a meridian,  $M = \frac{a(1-e^2)}{\sqrt{(1-e^2 \sin^2 \varphi)^3}}$ , where  $a$  is semimajor

axis of the ellipsoid of reference,  $e$  first eccentricity of the ellipsoid and  $\varphi$  latitude of a point

$N$

radius of curvature at a point on a parallel,  $N = \frac{a}{\sqrt{1-e^2 \sin^2 \varphi}}$ , where  $a$  is semimajor axis of

the ellipsoid of reference,  $e$  first eccentricity of the ellipsoid and  $\varphi$  latitude of a point